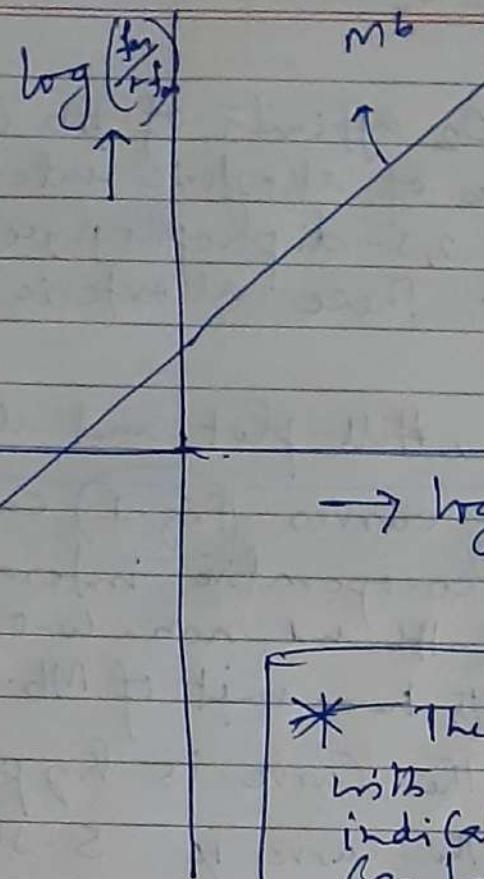


For Mb

Hill plot for Mb

(Non-cooperative)
slope

Lassonate
Page



$$\rightarrow \log \{ p(O_2) \}$$

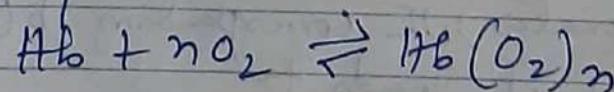
* The linear Hill plot with slope of unity indicates non-cooperativity (as for Mb)

$$\log \left(\frac{f_m}{1-f_m} \right) = \log \{ p(O_2) \} - \log P_{50}$$

slope = 1

For Hb :-

In case of Hb, the corresponding expressions are complicated and results are empirically formulated as follows for 1.5 process



$$K_H = \frac{[Hb(O_2)_n]}{[Hb] \{ p(O_2) \}^n} = \frac{f_H}{(1-f_H) \{ p(O_2) \}^{n-1}} = \frac{1}{(P_{50})^n}$$

$$\text{Then, } f_H = K_H \frac{\{ p(O_2) \}^n}{[1 + K_H \{ p(O_2) \}^n]}$$

$$\therefore \log \frac{f_H}{1-f_H} = n \log \{ p(O_2) \} + \log K_H = n \log \{ p(O_2) \} - n \log (P_{50})$$

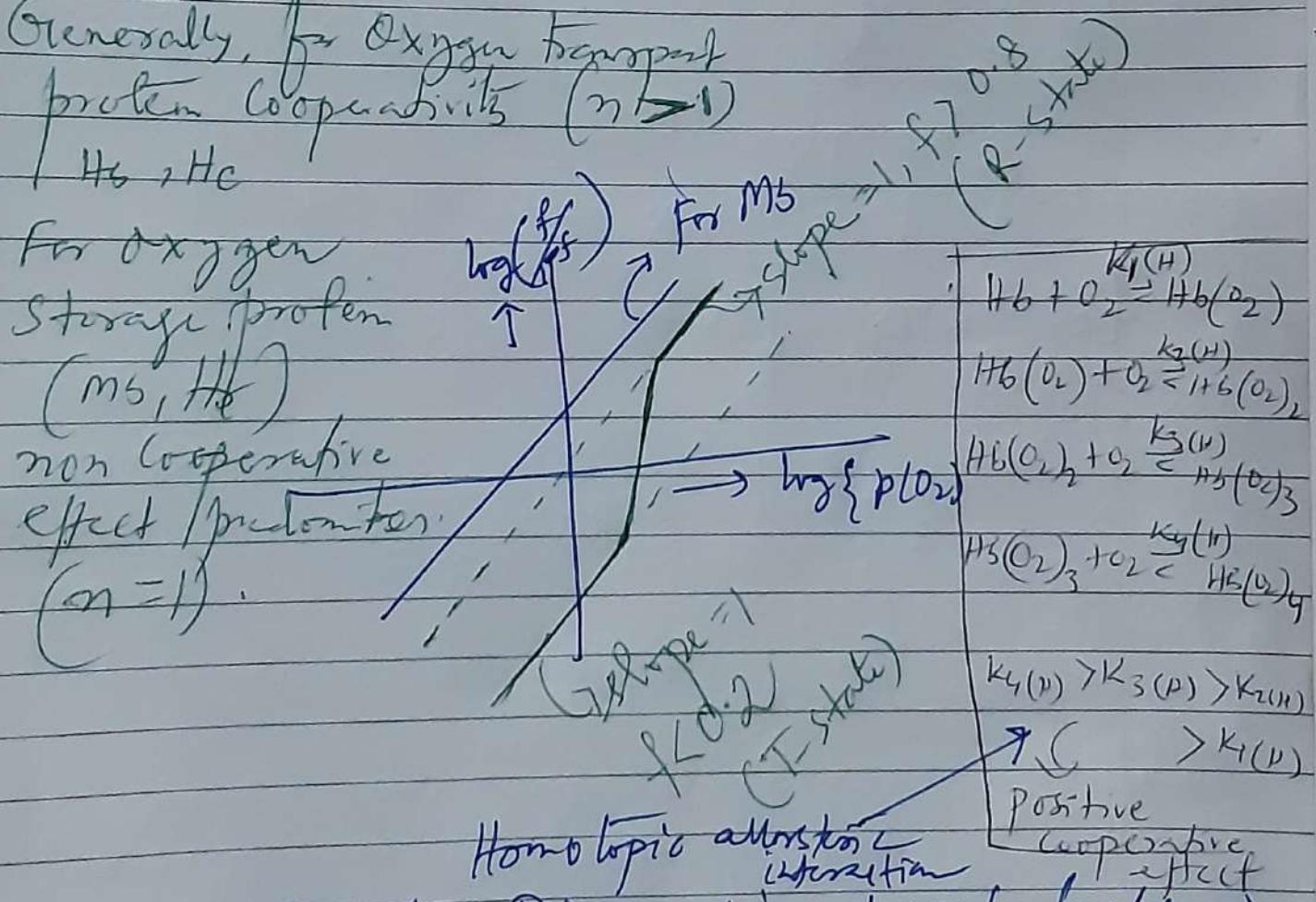
For Hb, $n > 1$, and it indicates that O₂-binding in the subunits of Hb is ~~independent~~ interdependent and it suggests positive cooperativity among the heme units due to heme-heme interaction.

To characterize the co-operativity for Hb, the O₂ binding data at intermediate saturation (i.e., $0.2 < f < 0.8$) yield a straight ~~line~~ line in Hill plot with a slope close to 3.

$$f < 0.2 \text{ or } f > 0.8 \quad (\text{No cooperativity}) \\ \text{i.e., } n=1$$

* Generally, for Oxygen transport protein cooperativity ($n > 1$)

Hb > Hc



* Will be Discussed in next lecture \Rightarrow

- Home tasks:
- ① What is T State & R-State?
 - ② What is α -chain & β -Chain
 - ③ What is Trigged mechanism?
 - ④ What is Soret Band & β -band?
 - ⑤ What are their position in UV-VIS spectrum and spin states in deoxy Hb & O₂-Hb.

3. Elementary quantum mechanics

Q-1 :- Define Black-body radiation and explain its characteristics features.

Q-2 :- Explain the Planck's Quantum Theory.

Q-3 :- Define photoelectric effect and explain the law of photoelectric emission.

Q-4 :- Derive Einstein photo emissions equation.

► Q-5 :- Explain the de-Broglie's hypothesis.

Q-6 :- Derive time independent Schrödinger equation.

Q-7 :- State and explain Heisenberg's uncertainty principle.

Q-8 :- Derive time dependent Schrödinger equation.

Q-9 :- Give the physical significance of $\Psi(x, y, z, t)$ and $\Psi^*(x, y, z, t)$

Q-10 :- What is normalized wave function.

► Q-11 :- State the basic postulates of quantum mechanics.

Q-12 :- What is an operator?

Q-13 :- Define linear operator?

Q-14 :- Enlighten the rules for setting up quantum mechanical operators.

Q-15 :- What is Commutator of the operators?

Q-16 :- Evaluate the following commutators.

$$[\hat{x}, \frac{d}{dx}], [\hat{x}, \hat{p}_x], [\frac{\partial}{\partial x}, \frac{\partial}{\partial y}], [\hat{x}, \hat{H}_x], [\hat{p}_x, \hat{H}_x]$$

$$[\hat{p}_x^2, \hat{x}^2],$$

Q-17 :- What is Eigen value equation?

Q-18 :- Which of the following functions

$$\sin 3x$$

$$x \sin x$$

$$3e^{-5x}$$

are eigen function of the operator $\frac{\partial^2}{\partial x^2}$.

Q-19 :- Show that e^{ikx} and e^{-ikx} are eigen function of one dimensional linear momentum operator and what are the corresponding eigen values?

Q-20 :- What is stationary States?

Q-21 :- What are the characteristics that must be satisfied by a function to be a eigen?

Q-22 :- Indicate which of the following function are acceptable wave function:

- i) $\psi = x$, ii) $\psi = x^2$, iii) $\psi = e^x$, iv) $\psi = e^{-x}$; v) $\psi = e^{-x^2}$
- vi) $\sin^{-1}x (-1, 1)$

Q-23 :- Prove that if \hat{A} and \hat{B} are two linear operator then $(\hat{A} + \hat{B})$ and $\hat{A}\hat{B}$ are also linear operators.

Q-24 :- Which of the following wave function are acceptable in quantum mechanics.

- i) $\sin x$, ii) $\tan x$, iii) $\cosec x$ iv) $\sin x + \cos x$

Q-25 :- If ψ_1 and ψ_2 are eigen functions of linear operator \hat{A} with same eigen values a , show that any linear combination of ψ_1 and ψ_2 will be also be an eigen function of \hat{A} with same eigen value.

Q-26 :- If $\psi_1(x,t)$ and $\psi_2(x,t)$ are both solutions of time dependent Schrodinger wave equation for a given potential $V(x)$. Show that $\Psi(x,t) = a_1\psi_1 + a_2\psi_2$ is also a solution, where a_1 and a_2 are constant.

Q-27 :- Define Hermitian Operator? What is the condition for an operator to be Hermitian?

Q-28 :- Check the following operator whether Hermitian or Anti-Hermitian in nature.

- i) $\frac{d}{dx}$, ii) $\frac{d^2}{dx^2}$, iii) \hat{P}_x , iv) \hat{H}_x , v) $\hat{\alpha}\hat{\beta} - \hat{\beta}\hat{\alpha}$ { $\hat{\alpha}, \hat{\beta}$ }
operator
- vi) $i(\hat{\alpha}\hat{\beta} - \hat{\beta}\hat{\alpha})$ { $\hat{\alpha}, \hat{\beta}$ }
operator

Q-29:- If two operators \hat{A}, \hat{B} are Hermitian, then find out its conditions, when $\hat{A}\hat{B}$ will be Hermitian.

Q-30:- What is orthonormal wave function?

Q-31:- Prove that eigen values of Hermitian operators are real.

Q-32:- If $\hat{A} \& \hat{B}$ are a pair of Commuting Hermitian operators, then they possess a common set of eigen functions.

Q-33:- If two Hermitian operators $\hat{A} \& \hat{B}$ possess a common set of eigen functions ψ_i - then they commute.

Q-34:- If $\psi_m(x) \& \psi_n(x)$ are non-degenerate eigen functions of a Hermitian operator then they are orthogonal.

Q-35:- Write down the Schrödinger's wave equation of a free particle moving in one dimensional box and find out the wave functions and also calculate the allowed energy.

Q-36:- Find out the normalised wave function for free particle moving in one dimensional potential box.

Q-37:- Show that the free particle wavefunctions are orthogonal with each other.

Q-38:- Draw the wave function of free particle for $n=1, 2, 3$.

Q-39:- Draw the probability function of free particle for $n=1, 2, 3$.

Q-40:- Is the energy of a free particle quantized? Justify.

\checkmark Q-41 :- What is Zero point energy of free particle?

\checkmark Q-42 :- Show that The energy of the free particle is in the agreement with the uncertainty principle.

\checkmark Q-43 :- Discuss the motion of a free particle in the three dimensional potential box.

\checkmark Q-44 :- For a particle in a cubical box, write down the energy value for the condition, $n_x + n_y + n_z = 4$ and indicate the level of degeneracy if any.

\checkmark Q-45 :- Evaluate the expectation value of K.E of a free particle in an one dimensional potential box of length 'l'.

\checkmark Q-46 :- Calculate the expectation value of $\langle \hat{x} \rangle$, $\langle \hat{x}^2 \rangle$, $\langle \hat{p}_x \rangle$ and $\langle \hat{p}_x^2 \rangle$ for a particle in a one dimensional box of width 'l' and infinitely high potential walls with origin at the end of the box.

\checkmark Q-47 :- Derive the energy expression of Simple Harmonic Oscillator (SHO).

\checkmark Q-48 :- Show that the energy zero point energy of the simple harmonic oscillator is consistent with the uncertainty principle.

* Q-49 :- Verify that the function $A \cdot \exp\left(\frac{1}{2}\beta x^2\right)$ is an eigen-function of a linear harmonic oscillator, where $\beta = (m\omega)^{1/2}/h$

Q-50 :- Write down the Schrödinger time independent equation of wave for H atom in terms of both Cartesian & polar co-ordinates.

* Q-51 :- Show that energy of H-atom is n^2 -fold degenerate.

Q-52 :- Show that H-atom wave functions are orthogonal to each other.

Q-53 :- What is Sinusoidal wave function?

Q-54:- From the probability density of $1s$ e^- , show that the most probable distance of e^- from the nucleus is equal to Bohr radius.

$$\Psi_{1s} = \frac{1}{(\pi a_0^3)^{1/2}} e^{-r/a_0}, \text{ where } a_0 \text{ is the Bohr radius.}$$

Q-55:- For the $2s$ state of H atom,

$\Psi_{2s} = \frac{1}{\sqrt{32\pi}} (2-r).e^{-r/2}$ in a.u., find the most probable and the nodal distances of the electron from the nucleus.

Q-56:- Normalize the ground state wave function for one dimensional harmonic oscillator $\Psi_0 = f(x) = A \cdot e^{-\frac{\beta x^2}{2}}$ where $\beta = \frac{(m\kappa)^{1/2}}{\hbar}$

Q-57:- Show that the following two wave functions are orthogonal to each other. $\Psi_0(x) = \left(\frac{\beta}{\pi}\right)^{1/4} e^{-\frac{\beta x^2}{2}}$ and $\Psi_1(x) = \left(\frac{4\beta^3}{\pi}\right) x \cdot e^{-\frac{\beta x^2}{2}}$, β is a constant.

Q-58:- Derive the bonding & antibonding orbital wavefunction for sp , sp^2 & sp^3 orbital.

Q-59:- Define radial wave function & angular wave function.

Q-60:- What is Linear Combination of Atomic Orbital. Explain with example.