

$$\begin{aligned}\Delta^2 f(x) &= 88 \times h \times 3x^{(2)} + 822 \times h \times 2x^{(1)} + 1360 \times h \\ &= 88 \times 2 \times 3x^{(2)} + 822 \times 2 \times 2x^{(1)} + 1360 \times 2 \\ &= 528x^{(2)} + 3288x^{(1)} + 2720\end{aligned}$$

$$\begin{aligned}\Delta^3 f(x) &= 528 \times h \times 2x^{(1)} + 3288 \times h \\ &= 528 \times 2 \times 2x^{(1)} + 3288 \times 2 \\ &= 2112x^{(1)} + 6576\end{aligned}$$

$$\begin{aligned}\Delta^4 f(x) &= 2112 \times h \\ &= 2112 \times 2 \\ &= 4224\end{aligned}$$

2nd Method :

Using Synthetic division rule

$$\begin{aligned}\text{let } f(x) &= 11x^4 + 5x^3 + 2x^2 + x - 15 \\ &= 11x^{(4)} + Ax^{(3)} + Bx^{(2)} + Cx^{(1)} + D\end{aligned}$$

2	11	5	2	1	-15 = D
		22	54	112	
4	11	27	56	113 = C	
		44	284		
6	11	71	340 = B		
		66			
	11	137 = A			

$$\therefore f(x) = 11x^{(4)} + 137x^{(3)} + 340x^{(2)} + 113x^{(1)} - 15$$