

Mathematical problems \Rightarrow (Molar polarization)

A liquid of mol. wt. 18 and density $0.995 \times 10^3 \text{ Kg m}^{-3}$ at 25°C has a dielectric Constant 78.5 and refractive index 1.383. Calculate the values of its molar polarisation, molar refractance and dipole moments, neglecting atomic polarisation.



$$\begin{aligned}\text{Density, } \rho &= 0.995 \times 10^3 \text{ Kg/m}^3 \\ &= 0.995 \times 10^3 (10^3 \text{ gm}) / (10^2 \text{ cm})^3 \\ &= 0.995 \text{ gm/cm}^3\end{aligned}$$

\therefore Molar polarisation,

$$P_M = \frac{D-1}{D+2} \cdot \frac{M}{\rho}$$

(D = Dielectric Constant)

$$= \frac{78.5-1}{78.5+2} \times \frac{18}{0.995} = 17.416 \text{ c.c.}$$

Molar refraction,

$$R_M = \frac{n^2-1}{n^2+2} \cdot \frac{M}{\rho} \quad \left(n = \text{refractive index of the said liquid} \right)$$

$$\begin{aligned}&= \frac{(1.383)^2-1}{(1.383)^2+2} \times \frac{18}{0.995} \\ &= 4.2199 \text{ c.c.}\end{aligned}$$

Orientation polarisation,

$$P_o = P_M - R_M$$

$$= (17.416 - 4.2199) \text{ c.c.}$$

$$= 13.1961 \text{ c.c.}$$

$$\boxed{P_M = P_o + P_e + P_a}$$

Since P_a is neglected

$$\underline{P_e = R_M}$$

$$\text{Again, } P_o = \frac{4}{3} \pi N_A \left(\frac{\mu^2}{3kT} \right)$$

$$\Rightarrow \mu^2 = \frac{9KT P_0}{4\pi N_A}$$

(μ = Dipole moment)

$$\mu = \left(\frac{9KT P_0}{4\pi N_A} \right)^{\frac{1}{2}}$$

$$\left\{ \begin{array}{l} K = 1.38 \times 10^{-16} \text{ erg K}^{-1} \\ T = 298 \text{ K} \\ N_A = 6.023 \times 10^{23} / \text{mole} \end{array} \right.$$

$$\therefore \mu = \left(\frac{9 \times 1.38 \times 10^{-16} \times 298 \times 13.961}{4 \times 3.14 \times 6.023 \times 10^{23}} \right)^{\frac{1}{2}}$$

$$= 8.035 \times 10^{-19} \text{ esu-cm}$$

$$= 0.8035 \times 10^{-18} \text{ esu-cm}$$

$$= \boxed{0.8035 \text{ D}}$$

Next lecture topic :-

- ① Debye equation
- ② Molar refraction (Lorentz-Lorentz equation)

Homeworks :-

The refractive index of CCl_4 for Sodium D light at 20°C is 1.457 and its density is 1.595 gm/cc . Calculate the molar refraction. If the atomic refraction of Carbon be 2.42, Calculate the atomic refraction of chlorine.