

Now according to 1st Law of Thermodynamics we may write

$$dU = dQ + dW$$

$$\checkmark C_p dT = C_v dT + p dv \quad (\text{By using eq}^n \text{(i)}, \text{(ii)}, \text{(iv)})$$

$$\checkmark C_p dT - C_v dT = p dv$$

$$\checkmark (C_p - C_v) dT = p dv \quad \text{--- (v)}$$

Since for one mole of an ideal gas we have

$$pV = RT$$

on differentiating both sides we get-

$$p dv = R dT \quad \text{--- (vi)} \quad \left(\begin{array}{l} p = \frac{RT}{V} \\ R = \text{const} \end{array} \right)$$

putting the value of eqⁿ (vi) in (v) we get-

$$\checkmark (C_p - C_v) dT = R dT$$

$$\checkmark \boxed{C_p - C_v = R} \quad \text{--- (vii)}$$

This eqⁿ (vii) is also known as Mayer's relation.

Note: Here C_p , C_v & R all are expressed in the same unit.